

# High School

## Math A

## Math B

### Some Manipulatives

Algebra tiles  
Dice  
Geometric models  
Tessellation tiles

Mirrors or miras  
Spinners  
Geoboards  
Conic section models

Volume demonstration kits  
Measuring tools  
Compasses  
PentaBlocks

### Calculator

Calculators will be *required* for use on Math A and B assessments. Scientific calculators are required for the Math A Regents examinations. Graphing calculators that do not allow for symbolic manipulation will be required for the Math B Regents examination and will be permitted (*not required*) for the Math A Regents examination starting in June 2000.

### Note

The Math A exam may include any given topic listed in the Core Curriculum with any performance indicator. The content includes most of the topics in the present Course I and a selection of topics from Course II. Programs other than Course I and II could be used as long as all the performance indicators and topics in the curriculum are part of the program. Examples of assessment items for Math A have been provided for most performance indicators. The items were taken from the 1997 pilot test and 1998 Test Sampler. Suggestions for classroom activities are substituted for any performance indicator that was not included in the sample test.

The Math B exam may include any given topic listed in the Core Curriculum with any performance indicator. Programs other than Course II and III could be used as long as the performance indicators and topics mentioned are part of the program. Since there is no Math B exam at this time, no assessment items have been included for Math B. Suggestions for possible classroom activities or problems are given instead to provide clarification of most performance indicators.

## Key Idea 1 Mathematical Reasoning

Students use mathematical reasoning to analyze mathematical situations, make conjectures, gather evidence, and construct an argument.

| PERFORMANCE INDICATORS                          | INCLUDES                                                                                                                                                                                                                                                                                                                                          | EXAMPLES                   |
|-------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 1A. Construct valid arguments.                  | <ul style="list-style-type: none"> <li>Truth value of compound sentences (conjunction, disjunction, conditional, related conditionals such as converse, inverse, and contrapositive, and biconditional).</li> <li>Truth value of simple sentences (closed sentences, open sentences with replacement set and solution set, negations).</li> </ul> | See Assessment Example 1A. |
| 1B. Follow and judge the validity of arguments. | <ul style="list-style-type: none"> <li>Truth value of compound sentences.</li> </ul>                                                                                                                                                                                                                                                              | See Assessment Example 1B. |

## **Key Idea 2**

### **Number and Numeration**

**M**ath A

Students use number sense and numeration to develop an understanding of the multiple uses of numbers in the real world, the use of numbers to communicate mathematically, and the use of numbers in the development of mathematical ideas.





## Key Idea 4 Modeling/Multiple Representation

### Continued

| PERFORMANCE INDICATORS                                                    | INCLUDES                                                                                                                                                                                                                                                                                                                   | EXAMPLES                   |
|---------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 4D. Develop and apply the concept of basic loci to compound loci.         | <ul style="list-style-type: none"> <li>• Locus.</li> <li>• At a fixed distance from a point.</li> <li>• At a fixed distance from a line.</li> <li>• Equidistant from two points.</li> <li>• Equidistant from two parallel lines.</li> <li>• Equidistant from two intersecting lines.</li> <li>• Compound locus.</li> </ul> | See Assessment Example 4D. |
| 4E. Model real-world problems with systems of equations and inequalities. | <ul style="list-style-type: none"> <li>• Systems of linear equations and inequalities.</li> </ul>                                                                                                                                                                                                                          | See Assessment Example 4E. |

## Key Idea 5 Measurement

## M<sup>ath</sup> A

Students use measurement in both metric and English measure to provide a major link between the abstractions of mathematics and the real world in order to describe and compare objects and data.

| PERFORMANCE INDICATORS                                                                                            | INCLUDES                                                                                                                                                                                                                                                                                                                                                                         | EXAMPLES                   |
|-------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 5A. Apply formulas to find measures such as length, area, volume, weight, time, and angle in real-world contexts. | <ul style="list-style-type: none"> <li>Perimeter of polygons and circumference of circles.</li> <li>Area of polygons and circles.</li> <li>Volume of solids.</li> <li>Pythagorean theorem.</li> </ul>                                                                                                                                                                            | See Assessment Example 5A. |
| 5B. Choose and apply appropriate units and tools in measurement situations.                                       | <ul style="list-style-type: none"> <li>Converting to equivalent measurements within metric and English measurement systems.</li> <li>Direct and indirect measure.</li> </ul>                                                                                                                                                                                                     | See Classroom Idea 5B.     |
| 5C. Use dimensional analysis techniques.                                                                          | <ul style="list-style-type: none"> <li>Dimensional analysis.</li> </ul>                                                                                                                                                                                                                                                                                                          | See Assessment Example 5C. |
| 5D. Use statistical methods including the measures of central tendency to describe and compare data.              | <ul style="list-style-type: none"> <li>Collecting and organizing data: sampling, tally, chart, frequency table, circle graphs, broken line graphs, frequency histogram, box and whisker plots, scatter plots, stem and leaf plots, and cumulative frequency histogram.</li> <li>Measures of central tendency: mean, median, mode.</li> <li>Quartiles and percentiles.</li> </ul> | See Assessment Example 5D. |
| 5E. Use trigonometry as a method to measure indirectly.                                                           | <ul style="list-style-type: none"> <li>Right triangle trigonometry.</li> </ul>                                                                                                                                                                                                                                                                                                   | See Assessment Example 5E. |
| 5F. Apply proportions to scale drawings and direct variation.                                                     | <ul style="list-style-type: none"> <li>Ratio.</li> <li>Proportion.</li> <li>Scale drawings.</li> <li>Percent.</li> <li>Similar figures.</li> <li>Similar polygons: ratio of perimeters and areas.</li> <li>Direct variation.</li> </ul>                                                                                                                                          | See Assessment Example 5F. |
| 5G. Relate absolute value, distance between two points, and the slope of a line to the coordinate plane.          | <ul style="list-style-type: none"> <li>Absolute value and length of a line segment.</li> <li>Midpoint of a segment.</li> <li>Equation of a line: point-slope and slope intercept form.</li> <li>Comparison of parallel and perpendicular lines.</li> </ul>                                                                                                                       | See Assessment Example 5G. |

| PERFORMANCE INDICATORS                                                                         | INCLUDES                                                                                                                                        |  |
|------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------|--|
| 5H. Explain the role of error in measurement and its consequence on subsequent calculations.   | <ul style="list-style-type: none"> <li>Error of measurement and its consequences on calculation of perimeter of polygons and circum-</li> </ul> |  |
| 5I. Use geometric relationships in relevant measurement problems involving geometric concepts. |                                                                                                                                                 |  |



### Key Idea 7

#### Patterns/Functions

Students use patterns and functions to develop mathematical power, appreciate the true beauty of mathematics, and construct generalizations that describe patterns simply and efficiently.

| PERFORMANCE INDICATORS                                                                          | INCLUDES                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | EXAMPLES                   |
|-------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 7A. Represent and analyze functions, using verbal descriptions, tables, equations, and graphs.  | <ul style="list-style-type: none"> <li>Techniques for solving equations and inequalities.</li> <li>Techniques for solving factorable quadratic equations.</li> <li>Graphs of linear relations: slope and intercept.</li> <li>Graphs of conics: circle and parabola.</li> <li>Graphic solution of systems of linear equations, inequalities, and quadratic-linear pair.</li> <li>Algebraic solution of systems of linear equations, inequalities, and quadratic-linear pair by substitution method and addition-subtraction method.</li> </ul> | See Assessment Example 7A. |
| 7B. Apply linear and quadratic functions in the solution of problems.                           | <ul style="list-style-type: none"> <li>Graphic and algebraic solutions of linear and quadratic functions in the solution of problems.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                              | See Assessment Example 7B. |
| 7C. Translate among the verbal descriptions, tables, equations, and graphic forms of functions. | <ul style="list-style-type: none"> <li>Translate linear and quadratic functions, systems of equations, inequalities and quadratic linear pairs between representations that are verbal descriptions, tables, equations, or graphs.</li> </ul>                                                                                                                                                                                                                                                                                                 | See Assessment Example 7C. |
| 7D. Model real-world situations with the appropriate function.                                  | <ul style="list-style-type: none"> <li>Determine and model real-life situations with appropriate functions.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                                        | See Assessment Example 7D. |
| 7E. Apply axiomatic structure to algebra.                                                       | <ul style="list-style-type: none"> <li>Solve linear equations with integral, fraction, or decimal coefficients.</li> <li>Solve linear inequalities.</li> <li>Solve factorable quadratic equations.</li> <li>Solve systems of linear equations, inequalities, and quadratic-linear pair.</li> </ul>                                                                                                                                                                                                                                            | See Assessment Example 7E. |



Show how you arrived at your answer.

1B.

“If Mary and Tom are classmates, then they go to the same school.”

Which statement below is logically equivalent?

- A. If Mary and Tom do not go to the same school, then they are not classmates.
- B. If Mary and Tom are not classmates, then they do not go to the same school.
- C. If Mary and Tom go to the same school, then they are classmates.
- D. If Mary and Tom go to the same school, then they are not classmates.

2A.

A clothing store offers a 50% discount at the end of each week that an item remains unsold. Patrick wants to buy a shirt at the store and he says, “I’ve got a great idea! I’ll wait two weeks, have 100% off, and get it for free!” Explain to your friend Patrick why he is incorrect, and find the correct percent of discount on the original price of a shirt.

2B.

For what value  $t$  is  $\frac{1}{\sqrt{t}} < \sqrt{t} < t$  true?

- A. 1
- B. 0
- C. -1
- D. 4

**3A.**

Mr. Cash bought  $d$  dollars worth of stock. During the first year, the value of the stock tripled. The next year, the value of the stock decreased by \$1,200.

***Part A***

Write an expression in terms of  $d$  to represent the value of the stock after two years.

***Part B***

If an initial investment is \$1,000, determine its value at the end of 2 years.

**3B.**

# ASSESSMENT EXAMPLES

## EXAMPLES FOR

### Math A

**M**ath A

4A.

A 10-foot ladder is placed against the side of a building as shown in Figure 1 below. The bottom of the ladder is 8 feet from the base of the building. In order to increase the reach of the ladder against the building, it is moved 4 feet closer to the base of the building as shown in Figure 2.

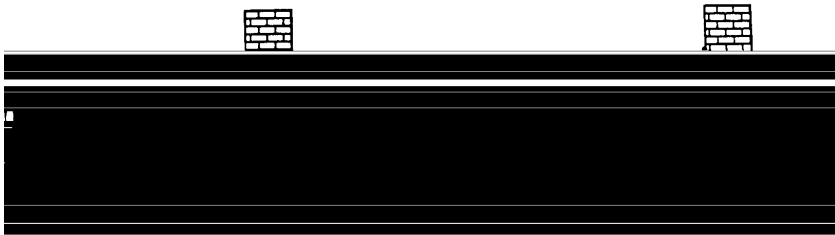


Figure 1

Figure 2

To the *nearest foot*, how much farther up the building does the ladder now reach?

**Show how you arrived at your answer.**

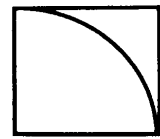
**Show how you arrived at your answer.**

5A.

Ms. Brown plans to carpet part of her living room floor. The living room floor is a square 20 feet by 20 feet. She wants to carpet a quarter-circle as shown below.

Find, to the *nearest square foot*, what part of the floor will remain uncarpeted.

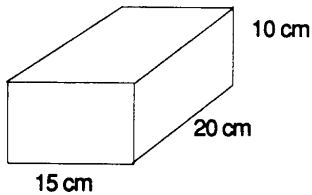
**Show how you arrived at your answer.**



20'

5C.

Jed bought a generator that will run for 2 hours on a liter of gas. The gas tank on the generator is a rectangular prism with dimensions 20 centimeters by 15 centimeters by 10 centimeters as shown below.



If Jed fills the tank with gas, how long will the generator run?

**Show how you arrived at your answer.**

5D.

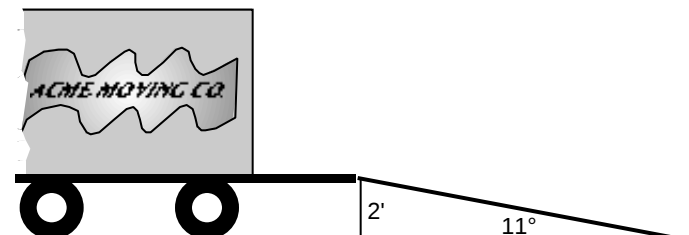
On his first 5 biology tests, Bob received the following scores: 72, 86, 92, 63, and 77. What test score must Bob earn on his sixth test so that his average (mean) for all six tests will be 80%?

**Show how you arrived at your answer.**

5E.

The tailgate of a truck is 2 feet above the ground. The incline of a ramp used for loading the truck is  $11^\circ$ , as shown.

Find, to the *nearest tenth of a foot*, the length of the ramp.



# ASSESSMENT EXAMPLES

## EXAMPLES FOR

### Math A

# M<sup>ath</sup> A

5F.

Joan has two square garden plots. The ratio of the lengths of the sides of the two squares is 2:3. What is the ratio of their areas?

- A. 2:3
- B. 3:2
- C. 4:9
- D. 9:4

5G.

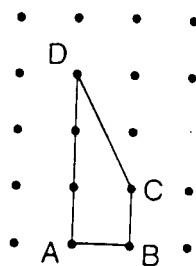
What is the distance between points A (7,3) and B (5,-1)?

(1)  $\sqrt{10}$   
(2)  $\sqrt{12}$

(3)  $\sqrt{14}$   
(4)  $\sqrt{20}$

5I.

In the figure shown below, each dot is one unit from an adjacent horizontal or vertical dot.



Find the number of square units in the area of quadrilateral ABCD.

**Show how you arrived at your answer.**

**6B.**

Paul is playing a game in which he rolls two regular six-sided dice. What is the probability that he will roll two doubles in a row?

**6C.**

The graph below shows the hair colors of all the students in a class.

What is the probability that a student chosen at random from this class has black hair?

**6D.**

Erica cannot remember the correct order of the four digits in her ID number. She does remember that the ID number contains the digits 1, 2, 5, and 9. What is the probability that the first three digits of Erica's ID number will all be odd numbers?

- A.  $\frac{1}{4}$
- B.  $\frac{1}{3}$
- C.  $\frac{1}{2}$
- D.  $\frac{3}{4}$

# ASSESSMENT EXAMPLES

EXAMPLES FOR

**M**ath A



# CLASSROOM IDEAS

## EXAMPLES FOR

### Math A

**M**ath A

*The following ideas for lessons and activities are provided to illustrate examples of each performance indicator. It is not intended that teachers use these specific ideas in their classrooms; rather, they should feel free to use them or adapt them if they so desire. Some of the ideas incorporate topics in science and technology. In those instances the appropriate standard will be identified. Some classroom ideas exemplify more than one performance indicator. Additional relevant performance indicators are given in brackets at the end of the description of the classroom idea.*

2C.

•

**5B.**

While watching a TV detective show, you see a crook running out of a bank carrying an attaché case. You deduce from the conversation of the two stars in the show that the robber has stolen \$1 million in small bills. Could this happen? Why or why not?

Hints: 1. An average attaché case is a rectangular prism (18" x 5" x 13").  
2. You might want to decide the smallest denomination of bill that will work.

[Also 5A.]

**5H.**

An odometer is a device that measures how far a bicycle (or a car) travels. Sometimes an odometer is not adjusted accu

### Key Idea 1

#### Mathematical Reasoning

# M

## Math B

Students use mathematical reasoning to analyze mathematical situations, make conjectures, gather evidence, and construct an argument.

| PERFORMANCE INDICATORS                             | INCLUDES                                                                                | EXAMPLES                   |
|----------------------------------------------------|-----------------------------------------------------------------------------------------|----------------------------|
| 1A. Construct proofs based on deductive reasoning. | <ul style="list-style-type: none"> <li>Euclidean and analytic direct proofs.</li> </ul> | See Classroom Activity 1A. |
| 1B. Construct indirect proofs.                     | <ul style="list-style-type: none"> <li>Euclidean indirect proofs.</li> </ul>            | See Classroom Activity 1B. |
|                                                    |                                                                                         |                            |

### Key Idea 2

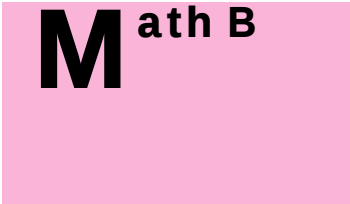
### Number and Numeration

Students use number sense and numeration to develop an understanding of the multiple uses of numbers in the real world, the use of numbers to communicate mathematically, and the use of numbers in the development of mathematical ideas.

| PERFORMANCE INDICATORS                                                      | INCLUDES                                                                                                                                                                                                                                                                                                  | EXAMPLES                   |
|-----------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 2A. Understand and use rational and irrational numbers.                     | <ul style="list-style-type: none"> <li>Determine from the discriminant of a quadratic equation whether the roots are rational or irrational.</li> <li>Rationalize denominators.</li> <li>Simplifying of algebraic fractions with polynomial denominators.</li> <li>Simplify complex fractions.</li> </ul> | See Classroom Activity 2A. |
| 2B. Recognize the order of the real numbers.                                | <ul style="list-style-type: none"> <li>Give rational approximations of irrational numbers to a specific degree of accuracy.</li> </ul>                                                                                                                                                                    | See Classroom Activity 2B. |
| 2C. Apply the properties of the real numbers to various subsets of numbers. | <ul style="list-style-type: none"> <li>Use the properties of real numbers in the development of algebraic skills.</li> </ul>                                                                                                                                                                              | See Classroom Activity 2C. |
| 2D. Recognize the hierarchy of the complex number system.                   | <ul style="list-style-type: none"> <li>Subsets of complex numbers.</li> </ul>                                                                                                                                                                                                                             | See Classroom Activity 2D. |
| 2E. Model the structure of the complex number system.                       | <ul style="list-style-type: none"> <li>Imaginary unit of complex numbers.</li> <li>Standard form of complex numbers.</li> </ul>                                                                                                                                                                           | See Classroom Activity 2E. |

# Key Idea 3

## Operations



Students use mathematical operations and relationships among them to understand mathematics.

| PERFORMANCE INDICATORS                                                                                                   | INCLUDES                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | EXAMPLES |
|--------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|
| 3A. Use addition, subtraction, multiplication, division, and exponentiation with real numbers and algebraic expressions. | <ul style="list-style-type: none"> <li>Operations with fractions with polynomial denominators.</li> <li>Add and subtract rational fractions with monomial and binomial denominators.</li> </ul>                                                                                                                                                                                                                                                                                                                             |          |
| 3B. Develop an understanding of and use the composition of functions and transformations.                                | <ul style="list-style-type: none"> <li>Understand the general concept and symbolism of the composition of transformations.</li> <li>Apply the composition of transformations (line reflections, rotations, translations, glide reflections).</li> <li>Identify graphs that are symmetric with respect to the axes or origin.</li> <li>Isometries (direct, opposite).</li> <li>Applications to graphing (inverse functions, symmetry).</li> <li>Define and compute compositions of functions and transformations.</li> </ul> |          |
| 3C. Use transformations on figures and functions in the coordinate plane.                                                | <ul style="list-style-type: none"> <li>Apply transformations (line reflection, point reflection, rotation, translation, and dilation) on figures and functions in the coordinate plane.</li> <li>Use slope and midpoint to demonstrate transformations.</li> <li>Use the ideas of transformations to investigate relationships of two circles.</li> <li>Use translation and reflection to investigate the parabola.</li> </ul>                                                                                              |          |

| PERFORMANCE INDICATORS                                                                  | INCLUDES                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | EXAMPLES                   |
|-----------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 3D. Use rational exponents on real numbers and all operations on complex numbers.       | <ul style="list-style-type: none"> <li>• Absolute value of complex numbers.</li> <li>• Evaluate expressions with fractional exponents.</li> <li>• Basic arithmetic operations with complex numbers.</li> <li>• Simplify square roots with negative radicands.</li> <li>• Use the product of a complex number and its conjugate to express the quotient of two complex numbers.</li> <li>• Cyclic nature of the powers of <math>i</math>.</li> <li>• Solving quadratic equations.</li> <li>• Laws of rational exponents.</li> </ul> | See Classroom Activity 3D. |
| 3E. Combine functions, using the basic operations and the composition of two functions. | <ul style="list-style-type: none"> <li>• Determine the value of compound functions.</li> <li>• Pairs of equations.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                      | See Classroom Activity 3E. |
|                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                            |

## Key Idea 4

### Modeling/Multiple Representation

Students use mathematical modeling/ multiple representation to provide a means of presenting, interpreting, communicating, and connecting mathematical information and relationships.

| PERFORMANCE INDICATORS                                                                                                                 | INCLUDES                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | EXAMPLES                   |
|----------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 4A. Represent problem situations symbolically by using algebraic expressions, sequences, tree diagrams, geometric figures, and graphs. | <ul style="list-style-type: none"> <li>Express quadratic, circular, exponential, and logarithmic functions in problem situations algebraically.</li> <li>Use symbolic form to represent an explicit rule for a sequence.</li> <li>Definition and graph of an inverse variation (hyperbola).</li> </ul>                                                                                                                                                                                                                                                                                    | See Classroom Activity 4A. |
| 4B. Manipulate symbolic representations to explore concepts at an abstract level.                                                      | <ul style="list-style-type: none"> <li>Use positive, negative, and zero exponents and be familiar with the laws used in working with expressions containing exponents.</li> <li>In the development of the use of exponents, the students should review scientific notation and its use in expressing very large or very small numbers.</li> <li>Rewrite the equality <math>\log_b a = c</math> as <math>a = b^c</math>.</li> <li>Solve equations, using logarithmic expressions.</li> <li>Rewrite expressions involving exponents and logarithms.</li> <li>Compound functions.</li> </ul> | See Classroom Activity 4B. |
| 4C. Choose appropriate representations to facilitate the solving of a problem.                                                         | <ul style="list-style-type: none"> <li>Select exponential or logarithmic process to solve an equation.</li> <li>Recognize that a variety of phenomena can be modeled by the same type of function.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                             | See Classroom Activity 4C. |
| 4D. Develop meaning for basic conic sections.                                                                                          | <ul style="list-style-type: none"> <li>Circles.</li> <li>Parabolas.</li> <li>Using the intercepts, recognize the ellipse and non-rectangular hyperbola.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                                        | See Classroom Activity 4D. |
|                                                                                                                                        |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                            |

## Key Idea 4 Modeling/Multiple Representation

### Continued

| PERFORMANCE INDICATORS                                                    | INCLUDES                                                                                                                                                                                                                                                                                                                                                                       | EXAMPLES                   |
|---------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 4E. Model real-world problems with systems of equations and inequalities. | <ul style="list-style-type: none"> <li>Solve systems of equations: linear, quadratic, and linear-quadratic systems.</li> </ul>                                                                                                                                                                                                                                                 | See Classroom Activity 4E. |
| 4F. Model vector quantities both algebraically and geometrically.         | <ul style="list-style-type: none"> <li>The Law of Sines and the Law of Cosines can be used with a wide variety of problems involving triangles, parallelograms and other geometric figures in applications involving the resolution of forces both algebraically and geometrically.</li> </ul>                                                                                 | See Classroom Activity 4F. |
| 4G. Represent graphically the sum and difference of two complex numbers.  | <ul style="list-style-type: none"> <li>Represent the basic operations of addition and subtraction.</li> </ul>                                                                                                                                                                                                                                                                  | See Classroom Activity 4G. |
| 4H. Model quadratic inequalities both algebraically and graphically.      | <ul style="list-style-type: none"> <li>Use multiple representation to show inequalities algebraically and graphically to find the possible solutions.</li> </ul>                                                                                                                                                                                                               | See Classroom Activity 4H. |
| 4I. Model the composition of transformations.                             | <ul style="list-style-type: none"> <li>The composition of two line reflections when the two lines are parallel.</li> <li>The composition of two rotations about the same point.</li> <li>The composition of two translations.</li> <li>The composition of a line reflection and a translation in a direction parallel to the line of reflection (glide reflection).</li> </ul> | See Classroom Activity 4I. |

# Key Idea 4

## Modeling/Multiple Representation

### Continued

| PERFORMANCE INDICATORS                                                                          | INCLUDES                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | EXAMPLES                   |
|-------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 4J. Determine the effects of changing parameters of the graphs of functions.                    | <ul style="list-style-type: none"> <li>Be able to sketch the effects of changing the value of <math>a</math> in the function <math>y = a^x</math>. Characteristics to be emphasized are: <ul style="list-style-type: none"> <li>-the domain of an exponential function is the set of real numbers</li> <li>-the range of an exponential function is the set of positive numbers</li> <li>-the graph of any exponential function will contain the point <math>(0, 1)</math></li> <li>-the exponential function is one-to-one.</li> </ul> </li> <li>If <math>a &gt; 1</math>, the graph rises, but if <math>0 &lt; a &lt; 1</math>, the graph falls.</li> <li>The graphs of <math>y = a^x</math> and <math>y = a^{-x}</math>, <math>a &gt; 0</math>, and <math>a \neq 1</math>, are reflections of each other in the <math>y</math>-axis.</li> <li>The logarithmic function is the inverse of the exponential function with the following characteristics: <ul style="list-style-type: none"> <li>-since the exponential function is one-to-one, its inverse, the logarithmic function, exists</li> <li>-the domain of the logarithmic function is the set of positive real numbers</li> <li>-the range of the logarithmic function is the set of all real numbers</li> <li>-the graph of any logarithmic function will contain the point <math>(1, 0)</math>.</li> </ul> </li> <li>The graphs of <math>y = a^x</math> and <math>x = a^y</math>, <math>a &gt; 0</math>, and <math>a \neq 1</math>, are reflections of each other in the line <math>y = x</math>.</li> </ul> | See Classroom Activity 4J. |
| 4K. Use polynomial, trigonometric, and exponential functions to model real-world relationships. | <ul style="list-style-type: none"> <li>Recognize when a real-world relationship can be represented by a linear, quadratic, trigonometric, or exponential function.</li> <li>Solve real-world problems by using linear, quadratic, trigonometric, and exponential functions.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | See Classroom Activity 4K. |

### Continued

| PERFORMANCE INDICATORS                                                           | INCLUDES                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | EXAMPLES                   |
|----------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 4L. Use algebraic relationships to analyze the conic sections.                   | <ul style="list-style-type: none"> <li>Write the equation of a circle with a given center and radius and determine the radius and center of a circle whose equation is in the form <math>(x - h)^2 + (y - k)^2 = r^2</math>.</li> <li>Recognize an equation in the form <math>y = ax^2 + bx + c</math>, <math>a \neq 0</math> as an equation of a parabola and               <ul style="list-style-type: none"> <li>-be able to form a table of values in order to sketch its graph</li> <li>-find the axis of symmetry</li> <li>-determine the abscissa of the vertex to provide a point of reference for choosing the x-coordinates to be plotted</li> <li>-find the y-intercept of the parabola.</li> </ul> </li> <li>Turning point.</li> <li>Maximum or minimum.</li> </ul> | See Classroom Activity 4L. |
| 4M. Use circular functions to study and model periodic real-world phenomena.     | <ul style="list-style-type: none"> <li>Use the concept of the unit circle to solve real-world problems involving:               <ul style="list-style-type: none"> <li>-radian measure</li> <li>-sine</li> <li>-cosine</li> <li>-tangent</li> <li>-reciprocal trigonometric functions.</li> </ul> </li> <li>Relate reference angles, amplitude, period, and translations to the solution of real-world problems.</li> </ul>                                                                                                                                                                                                                                                                                                                                                     | See Classroom Activity 4M. |
| 4N. Use graphing utilities to create and explore geometric and algebraic models. | <ul style="list-style-type: none"> <li>Graph quadratic equations and observe where the graph crosses the x-axis, or note that it does not.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | See Classroom Activity 4N. |

## **Key Idea 5**

### **Measurement**

**M**ath B

Students use measurement in both metric and English measure to provide a major link between the abstractions of mathematics and the real world in order to describe and compare objects and data.





## Key Idea 6 Uncertainty

## M<sup>ath</sup> B

Students use ideas of uncertainty to illustrate that mathematics involves more than exactness when dealing with everyday situations.

| PERFORMANCE INDICATORS                                                                                                              | INCLUDES                                                                                                                                                                                                                                                                                                                | EXAMPLES                   |
|-------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 6A. Judge the reasonableness of results obtained from applications in algebra, geometry, trigonometry, probability, and statistics. | <ul style="list-style-type: none"> <li>Uses substitution as a check for solutions to equations and inequalities.</li> <li>Using proof as a check on the validity of geometric constructions.</li> <li>Compare histograms with formula-derived solutions for mean, median, variation, and standard deviation.</li> </ul> | See Classroom Activity 6A. |
| 6B. Judge the reasonableness of a graph produced by a calculator or computer.                                                       | <ul style="list-style-type: none"> <li>Determine the effects of changing the parameters of graphs of linear, quadratic, trigonometric, exponential, and circular functions.</li> </ul>                                                                                                                                  | See Classroom Activity 6B. |
| 6C. Interpret probabilities in real-world situations.                                                                               | <ul style="list-style-type: none"> <li>Applications of the probability of exactly, at least, or at most <math>r</math> successes in <math>n</math> trials of a Bernoulli experiment.</li> <li>Simple applications of the binomial theorem.</li> </ul>                                                                   | See Classroom Activity 6C. |
| 6D. Use a Bernoulli experiment to determine probabilities for experiments with exactly two outcomes.                                | <ul style="list-style-type: none"> <li>Definition of a Bernoulli experiment.</li> <li>Case where <math>r</math> successes are assumed to occur first.</li> <li>General case.</li> </ul>                                                                                                                                 | See Classroom Activity 6D. |
| 6E. Use curve fitting to fit data.                                                                                                  | <ul style="list-style-type: none"> <li>Linear, logarithmic, exponential, and power regressions from scatter plots.</li> <li>Linear correlation coefficient.</li> </ul>                                                                                                                                                  | See Classroom Activity 6E. |

| PERFORMANCE INDICATORS                                                                      | INCLUDES                                                                                                                                                                                                                                                                                                                                                                                              | EXAMPLES                   |
|---------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 6F. Create and interpret applications of discrete and continuous probability distributions. | <ul style="list-style-type: none"> <li>Measures of central tendency.</li> <li>Use of <math>\hat{\mu}</math>-notation.</li> <li>Measures of dispersion.</li> <li>Range.</li> <li>Mean absolute deviation.</li> <li>Variance using the calculator.</li> <li>Standard deviation using the calculator.</li> <li>Binomial theorem.</li> <li>Normal approximation for the binomial distribution.</li> </ul> | See Classroom Activity 6F. |
| 6G. Make predictions based on interpolations and extrapolations from data.                  | <ul style="list-style-type: none"> <li>Domain and range.</li> <li>Interpolate and extrapolate from graphs of linear, quadratic, trigonometric, circular, exponential, and logarithmic function.</li> </ul>                                                                                                                                                                                            | See Classroom Activity 6G. |

## Key Idea 7 Patterns/Functions

## Math B

Students use patterns and functions to develop mathematical power, appreciate the true beauty of mathematics, and construct generalizations that describe patterns simply and efficiently.

| PERFORMANCE INDICATORS                                                                          | INCLUDES                                                                                                                                                                                                                                                                                                                                     | EXAMPLES                   |
|-------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 7A. Use function vocabulary and notation.                                                       | <ul style="list-style-type: none"> <li>Definition of a relation.</li> <li>Determining if a relation is a function.</li> <li>Definition of inverse function.</li> <li>Notation for absolute value, composite functions.</li> <li>Expressing exponential functions as logs.</li> <li>Functions (inverse, exponential, logarithmic).</li> </ul> |                            |
| 7B. Represent and analyze functions, using verbal descriptions, tables, equations, and graphs.  | <ul style="list-style-type: none"> <li>Represent and analyze exponential, logarithmic, quadratic, and trigonometric functions.</li> </ul>                                                                                                                                                                                                    | See Classroom Activity 7B. |
| 7C. Translate among the verbal descriptions, tables, equations, and graphic forms of functions. | <ul style="list-style-type: none"> <li>Relate algebraic expressions to the graphs of functions.</li> </ul>                                                                                                                                                                                                                                   | See Classroom Activity 7C. |
| 7D. Analyze the effect of parametric changes on the graphs of functions.                        | <ul style="list-style-type: none"> <li>Use graphing calculators or sketches to analyze the effects of changing parameters of functions.</li> </ul>                                                                                                                                                                                           | See Classroom Activity 7D. |
| 7E. Apply linear, exponential, and quadratic functions in the solution of problems.             | <ul style="list-style-type: none"> <li>Solve real-world problems by using linear, exponential, and quadratic functions.</li> </ul>                                                                                                                                                                                                           | See Classroom Activity 7E. |
| 7F. Apply and interpret transformations to functions.                                           | <ul style="list-style-type: none"> <li>Use ideas of transformations to investigate the relationships between functions.</li> </ul>                                                                                                                                                                                                           | See Classroom Activity 7F. |
| 7G. Model real-world situations with the appropriate function.                                  | <ul style="list-style-type: none"> <li>Characteristics of linear, quadratic, trigonometric, circular, exponential, and logarithmic functions.</li> </ul>                                                                                                                                                                                     | See Classroom Activity 7G. |
| 7H. Apply axiomatic structure to algebra and geometry.                                          | <ul style="list-style-type: none"> <li>Algebraic and geometric proof.</li> <li>Find the solution of a quadratic equation both algebraically and graphically as a check.</li> <li>Use the quotient identities, reciprocal identities, and the Pythagorean identities.</li> </ul>                                                              | See Classroom Activity 7H. |

### Continued

| PERFORMANCE INDICATORS                                                                                             | INCLUDES                                                                                                                                                                                                                  | EXAMPLES                   |
|--------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|
| 7I. Solve equations with complex roots, using a variety of algebraic and graphical methods with appropriate tools. | <ul style="list-style-type: none"> <li>Determine from the discriminant of a quadratic equation whether the roots are imaginary, rational, or irrational.</li> </ul>                                                       | See Classroom Activity 7I. |
| 7J. Evaluate and form the composition of functions.                                                                | <ul style="list-style-type: none"> <li>Evaluate composite functions.</li> <li>Use composite functions in problem-solving situations.</li> </ul>                                                                           | See Classroom Activity 7J. |
| 7K. Solve equations, using fractions, absolute values, and radicals.                                               | <ul style="list-style-type: none"> <li>Fractional equations.</li> <li>Equations with radicals.</li> <li>Linear inequalities.</li> <li>Absolute value inequalities.</li> <li>Quadratic inequalities.</li> </ul>            | See Classroom Activity 7K. |
| 7L. Use basic transformations to demonstrate similarity and congruence of figures.                                 | <ul style="list-style-type: none"> <li>Transformations that provide congruence.</li> <li>Direct isometries.</li> <li>Opposite isometries.</li> <li>Transformations that provide similarity.</li> <li>Dilation.</li> </ul> | See Classroom Activity 7L. |
| 7M. Identify and differentiate between direct and indirect isometries.                                             | <ul style="list-style-type: none"> <li>Transformations that provide congruence.</li> </ul>                                                                                                                                | See Classroom Activity 7M. |
| 7N. Analyze inverse functions, using transformations.                                                              | <ul style="list-style-type: none"> <li>Identify inverse functions which are reflections in the line <math>y = x</math>.</li> </ul>                                                                                        | See Classroom Activity 7N. |
| 7O. Apply the ideas of symmetries in sketching and analyzing graphs of functions.                                  | <ul style="list-style-type: none"> <li>Simplify the graphing of functions by using symmetries with respect to an axis, the origin, or some other point.</li> </ul>                                                        | See Classroom Activity 7O. |
| 7P. Use the normal curve to answer questions about data.                                                           | <ul style="list-style-type: none"> <li>Standard deviation for grouped data.</li> <li>Measures of central tendency.</li> </ul>                                                                                             | See Classroom Activity 7P. |
| 7Q. Develop methods to solve trigonometric equations and verify trigonometric functions.                           | <ul style="list-style-type: none"> <li>Solve first-degree trigonometric equations.</li> <li>Solve quadratic trigonometric equations.</li> <li>Double- and half-angle formulas.</li> </ul>                                 | See Classroom Activity 7Q. |

## CLASSROOM IDEAS

### EXAMPLES FOR

#### Math B

**M**ath B

*The following ideas for lessons and activities are provided to illustrate examples of each performance indicator. It is not intended that teachers use these specific ideas in their classrooms; rather, they should feel free to use them or adapt them if they so desire. Some of the ideas incorporate topics in science and technology. In those instances the appropriate standard will be identified. Some classroom ideas exemplify more than one performance indicator. Additional relevant performance indicators are given in brackets at the end of the description of the classroom idea.*

1A.

Quadrilateral JAKE has coordinates  $J(0,3a)$ ,  $A(3a,3a)$ ,  $K(4a,0)$ , and  $E(-a,0)$ .

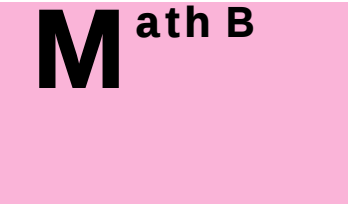
Prove by coordinate geometry that quadrilateral JAKE is an isosceles trapezoid.

1B.

For over 50 years Dorothy, the Tin Man, the Scarecrow, and the Lion have been following the yellow brick road in the *Wizard of Oz*. In the story, the scarecrow sings “I wish I had a brain” and goes off with Dorothy to the land of Oz in search of the Wizard who can hopefully satisfy this wish. As everyone knows, there really is no Wizard, but only a man pulling strings behind a curtain. Being a clever and kindhearted man, the ersatz wizard explains to the Scarecrow that he has had a brain all along but is only lacking a diploma to prove his intelligence. The Wizard then proceeds to bestow an honorary degree, with appropriate diploma, upon the Scarecrow. To demonstrate his newly discovered intelligence, the Scarecrow quotes the following theorem:

**The sum of the square roots of any two sides of an isosceles triangle is equal to the square root of the remaining side.**

Prove or disprove this theorem.



**CLASSROOM IDEAS**

**EXAMPLES FOR**

**Math B**

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# CLASSROOM IDEAS

## EXAMPLES FOR

### Math B

**M**ath B

3A.

A googol is a 1 followed by 100 zeros, and a googolplex is a 1 followed by a googol of zeros. Express these two numbers as powers of 10. [Also 3C.]

3B.

The Environmental Protection Agency has determined that in a certain section of the country the average level of air pollution is  $0.5 \div P + 10,000$  parts per million (ppm), where P is the population. The 1980 census predicts that the population t years after 1980 will be  $7000 + 40t^2$ .

A. Express the pollution level t years after 1980 as a composite function and reduce the composite function to a function of t.

B. What pollution level can be expected in 1990? 2000?

3C.

On graph paper, set up a coordinate system for each figure and graph the figure by plotting coordinates and connecting the points in order. Sketch the reflection of each shape over the line  $y = x$ .

a) (3,2), (-1,-4), (7,2), (-2,3); b) (1,7), (4,5), (6,-1); c) (-2,-4), (-1,5), (3,3); d) (6,4), (-2,5), (-2,-2), (3,5), (4, 2.5)

What is the relationship between the coordinates of the original figure and its reflection image? State your conjecture in if-then form. Write an argument that you could use with a friend to convince him/her that your conjecture is correct.

3D.

A. Convert  $6\sqrt{\frac{x^{42}y^{24}}{(-5)^6}}$  to exponential form and simplify.

B.  $i^4 i^5 i^6 = ?$

C. Simplify  $4 \div -18 + \div -50$

3E.

Cost Analysis: The cost C to produce x units of a given product per month is given by

$C = f(x) = 19,200 + 160x$ . If the demand x each month at a selling price of \$p per unit is given by

$x = g(p) = 200 - p/4$

Find  $(f \circ g)(p)$  and interpret.

# Math B

## CLASSROOM IDEAS

### EXAMPLES FOR

#### Math B

4A.

Draw the graph  $y = 48/x$  ( $x \neq 0$ ). Make a table, using some integral values of  $x$  from  $x = -16$  to  $x = 16$ . Identify the graph.

4B.

Prove: If  $x$  and  $n$  are real numbers, and  $x > 0$ , then  $\log_a (x^n) = n \log_a x$   $a > 0$ ,  $a \neq 1$ .

4C.

Students model population growth and decline of people, animals, bacteria, and decay of radioactive materials, using the appropriate exponential functions. [Also 4B.]

4D.

On your graphing calculator, graph the two conic sections on the same set of axes. Determine the number of points of intersection and estimate their value from the graph. Check your estimates by substitution. Discuss an allowable margin of error in the check.

$$\frac{x^2}{4} + \frac{y^2}{16} = 1$$

$$x^2 + y^2 = 9$$

4E.

Two toy rockets are launched, one ten seconds after the other. The height in feet of the first rocket after  $0 \leq t \leq 16$  seconds is given by  $h(t) = -16t^2 + 256t$ . The height of the second one after  $10 \leq t \leq 20$  seconds is given by  $g(t) = -16t^2 + 480t - 3200$ . How many seconds after the first rocket is launched are the rockets at the same height?

4F.

The weight of a plane wing is 750 lb. The drag is 300 lb. What is the magnitude and direction of the resulting force?

# CLASSROOM IDEAS

## EXAMPLES FOR

### Math B

**M**ath B

4G.

Have students investigate whether or not the difference of two complex conjugates can be a real number.

4H.

Solve the following inequality algebraically and graphically:  $x^2$





# Math B

## Key Idea 1 Mathematical Reasoning

### Assessment Examples

5G.

As one of its admissions criteria, a college requires an SAT math score that is among the top 70% (69.1%) of all scores. The mean score on the math portion of the SAT is 500 and the standard deviation is 100. What is the minimum acceptable score? Justify your answer by drawing a sketch of the normal distribution.

The mean score on the math portion of the SAT is 500 and the standard deviation is 100. What is the minimum acceptable score? Justify your answer by drawing a sketch of the normal distribution.

## CLASSROOM IDEAS

### EXAMPLES FOR

#### Math B

## M<sup>ath</sup> B

6A.

The following ads for truck rentals appear in the paper.

Easy Rent-A-Truck  
\$30 per day plus \$2 per mile

Fast Rent-A-Truck  
\$60 per day plus \$1 per mile

- A. You plan to rent a truck for one day. From which company would you rent? Why? Support your answer with a discussion of the factors you need to take into consideration. Use both equations and graphs to help illustrate your solution. Substitute specific values to check your results.
- B. Determine under what conditions, considering both days and milage, the expense of renting a truck from *Fast Rent-A-Truck* would be less expensive than renting from *Easy Rent-A-Truck*.

6B.

A rich philanthropist, who loved mathematics, agreed to sponsor an 18-hole golf tournament at the local country club. In order to enter, a contestant had to pay 2 cents and select either a linear, quadratic, or exponential formula to calculate how many CENTS he/she would receive for a winning hole. In each of the following formulas,  $x$  represents the number of the winning hole. linear,  $y = 2x$ ; quadratic,  $y = x^2$ , exponential,  $y = 2^x$ . Why bother entering if the payoff is in pennies? Use your graphing calculator to investigate. Describe numerically how the amounts change from one hole to the next for each method. Which method would you select on your entry form and why?

6C.

The principal of the local high school was willing to participate in the school fair dunking booth in which students who paid \$1 could push a button that operated a light over the booth which was programmed to flash either red or green. If the light flashed green, the principal would fall into the water. If it flashed red, he would not. He was told that the light was set to flash either red or green randomly with a 50% chance of turning green. As it turned out, the principal seemed to be dunked more than 50% of the time. In the first 20 pushes of the button, he was dunked 15 times. He was getting suspicious that probability had been misrepresented to him. Based on the results so far, do you think the principal has justification for being suspicious? What is your reasoning? If you do not think the principal is justified in his suspicions, how many occurrences of 75% dunks would it take to convince you that the light was not set at 50% green? If you think the principal is justified in being suspicious, what are the smallest occurrences of 75% that would be required to convince you? [Also Performance Indicators 6C., 6D., and 6E.]

**6D.**

If each problem can be regarded as a Bernoulli experiment, state the values of  $n$ ,  $p$ ,  $q$ , and  $r$ , and give the answer in symbolic form. If the problem cannot be regarded as a Bernoulli experiment, explain why. Four balls are drawn with replacement from an urn containing 4 red balls and 2 white balls.

What is the probability of drawing exactly 2 red balls?

Four balls are drawn without replacement from an urn containing 4 red balls and 2 white balls.

What is the probability of drawing exactly 2 red balls? [Also Performance Indicator 6F.]

**6E**

Given  $x = \{10, 20, 30, 40, 50\}$  and  $y = \{11.0, 12.1, 13.0, 13.9, 15.1\}$  where  $x$  is measured in lbs. force and  $y$  measures the length of a spring in inches.

- Find the equation which best fits the data.
- Determine the load when  $y = 17$  inches and determine the length of the spring when  $x = 62$  lbs.

**6F.**

In her algebra class, Ms. Goodheart predicts 8 of her 26 students will earn a score of 90 or above on a particular exam with a normal distribution. After taking the exam, the mean score was 84 with a standard deviation of 6. Was her prediction accurate? What should she have predicted to be more precise?

# CLASSROOM IDEAS

EXAMPLES FOR

Math B

**M**ath B

6G.

# Math B

## CLASSROOM IDEAS

### EXAMPLES FOR

#### Math B

7A.

$$f(x) = x^3 + 5$$

A. Does  $f(x)$  have an inverse?

B. If so, find the inverse and decide if it is a function

7B.

A projector throws an image on a screen. To determine how the width of the image is related to the distance of the screen from the projector, the following measurements were made.



Graph the data and find the equation relating  $x$  and  $y$ .

Find the width of the image when the projector is 3.0 m from the screen.

Find the distance from the projector to the screen when the image is 3.0 m wide.

What is the domain of the relation?

# CLASSROOM IDEAS

## EXAMPLES FOR

### Math B

**M**ath B

7E.

#### About Decay

Start this experiment with one cupful of M & M's. Shake the cup and pour the M & M's onto the napkin. Count the total number of M & M's. Write this as the number for trial #1. Then remove all M & M's that have the M showing. Record the total number left in the table below. Using the new total of M & M's each time, repeat the procedure five more times. Note if the number of M & M's reaches zero at any trial, the experiment is over at that time and you should not use the zero result as part of your data.

Create a scatterplot of Trial for x and total Number for y.

Enter the data in lists using your graphing calculator.

**Write the equation:**

Graph the exponential function on the grid above.

Use the equation to predict the number of M & M's you would have had two times before trial #1:

If there were a larger number of M & M's before trial #1, use the equation to predict the trial when there were 900 M & M's (a negative number):

Explain the coefficients a and b in the equation.

7G.

Nita Pass is about to study for a mathematics exam. Nita knows that the test grade is a function of the number of hours studied and knows from past experience that 1 hour of studying will result in a grade of 60; 2 hours, in a grade of 74; and 7 hours in a grade of 84.

Show Nita that the grade is not a linear function of the number of hours studied.

Assume that the grade varies quadratically with the number of hours studied. Find the equation for the function, and draw the graph (show important features: vertex and intercepts).

What is the minimum amount of study time needed to pass the test if the lowest passing grade is 70? What is the grade-intercept and what does it represent in the real world?

The quadratic model predicts that Nita could earn zero points on the test. What might happen in the real world that could actually cause her to score zero by studying this long?

Use the graph to show that there is no real value of time for which the grade will be 100.

7H.

Conjecture:

The angle bisector of the vertex angle of an isosceles triangle is also a median to the base.

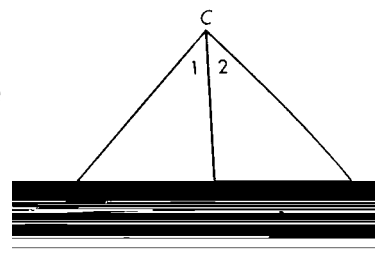
Given:

Isosceles  $\triangle ABC$  with  $\overline{AC} = \overline{BC}$  and with  $\overline{CD}$  an angle bisector of vertex angle  $C$ .

Show:

$\overline{CD}$  is a median to the base.

Two-column proof:



7I.

Solve the following equation for  $x$ :  $2x^2 + 5x - 1 = 0$ . Sketch the graph of the function  $y = 2x^2 + 5x - 1$ . Explain the relation between the roots of the equation and the  $x$ -intercepts of the graph of the function. [Also 3D., 4A., 6A., and 7C.]

# CLASSROOM IDEAS



The area  $A$  and perimeter  $P$  of a square are functions of its side length  $S$ . Express the area as a function of the perimeter.

The time it takes for a pendulum to swing back and forth once is called the period. This period  $T$  seconds is given by the formula,  $T = 2\pi\sqrt{l/g}$ , where  $l$  is the length of the pendulum in meters. By what factor is the period increased when the pendulum length is tripled?

7L.

Provide students with examples of Escher prints and have them identify two congruent shapes and the isometries that provide the congruence. [Also 4J.]

7M.

Note the tessellations below, using capital block letters T and E. Have students work in groups to:

- determine what transformations were used in these tilings.
- identify those that are direct or indirect isometries.
- determine what other capital block letters would tile a plane.
- use graph paper to create their tessellations and make a list describing their findings.

7N.

Graph each of the relations below, its inverse, and  $y = x$  on the same coordinate system. Which of the four relations are functions? Which of the inverses are functions?

$$\begin{array}{ll} g: y = 2x - 2 & f: y = -1/2x + 2 \\ p: y = x^2 + 1 & q: y = (x+2)^2 \end{array}$$

7O.

Find, if it exists, a line of symmetry of the graph of each equation. If there is no line of symmetry, write none.

$$y = x^2 + 5 \qquad y = x$$

7P.

The table below shows the scores on a writing test in an English class:

|       |  |
|-------|--|
| $X_i$ |  |
|       |  |
|       |  |
|       |  |
|       |  |
|       |  |